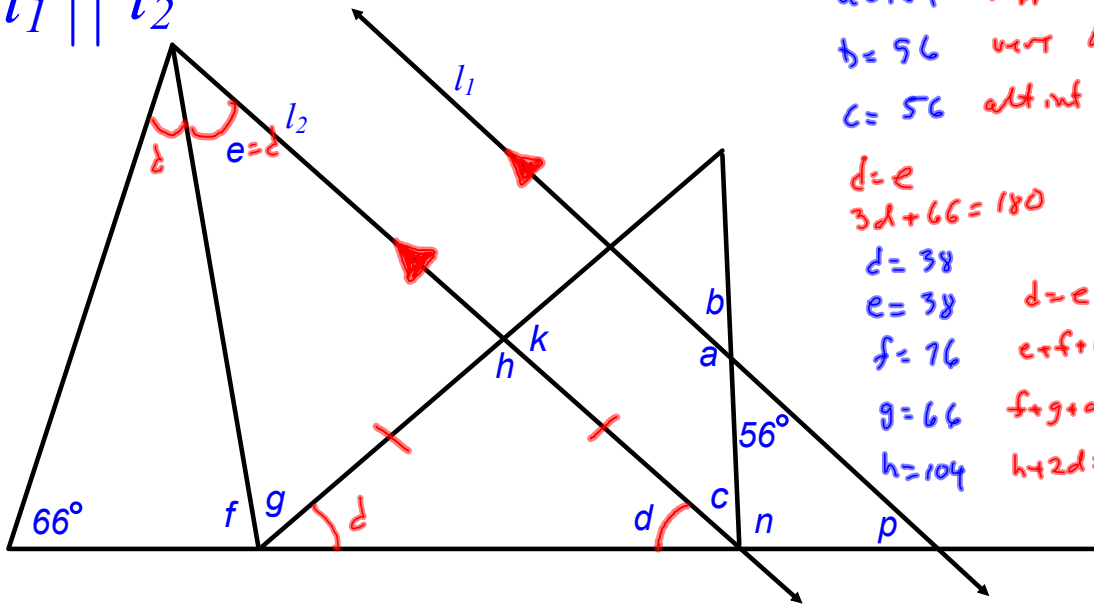


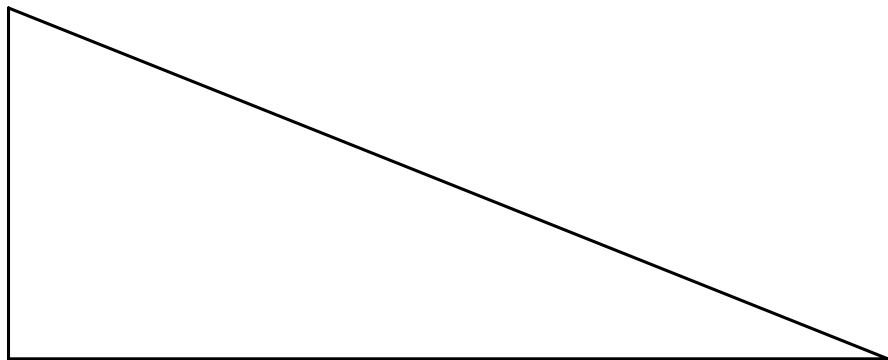
$l_1 \parallel l_2$

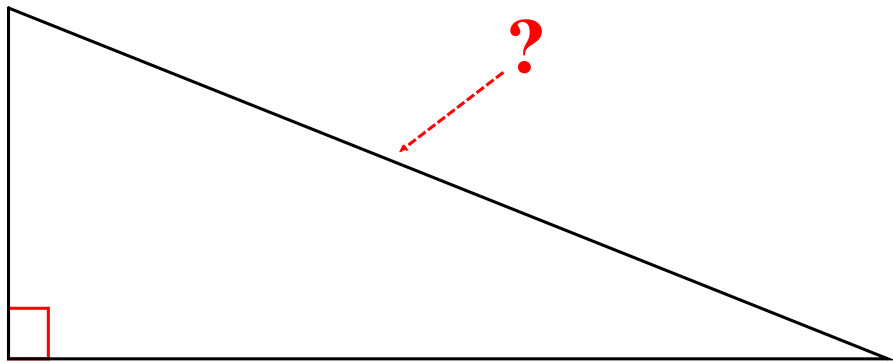
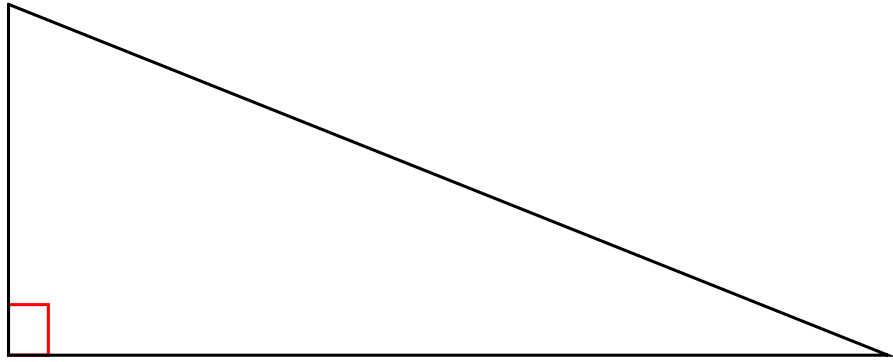


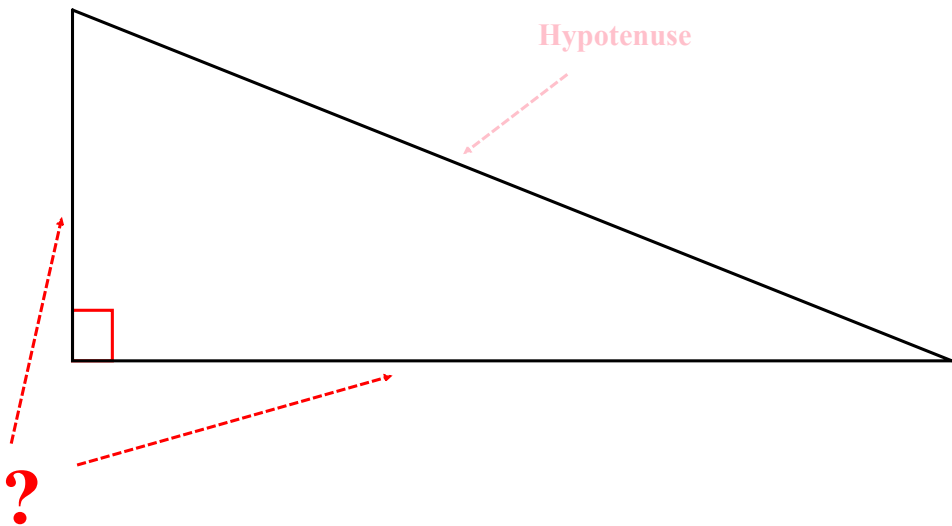
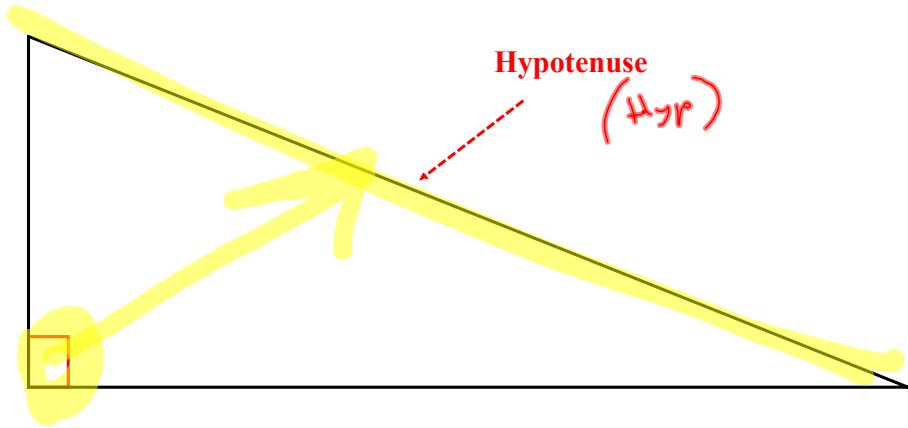
$a = 124$ suppl \angle 's
 $b = 56$ vert \angle 's
 $c = 56$ alt int \angle 's \parallel lines

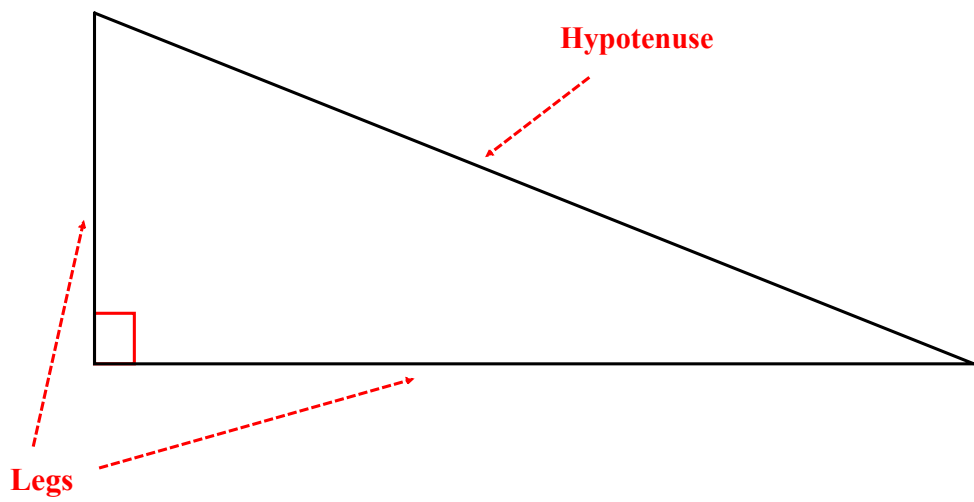
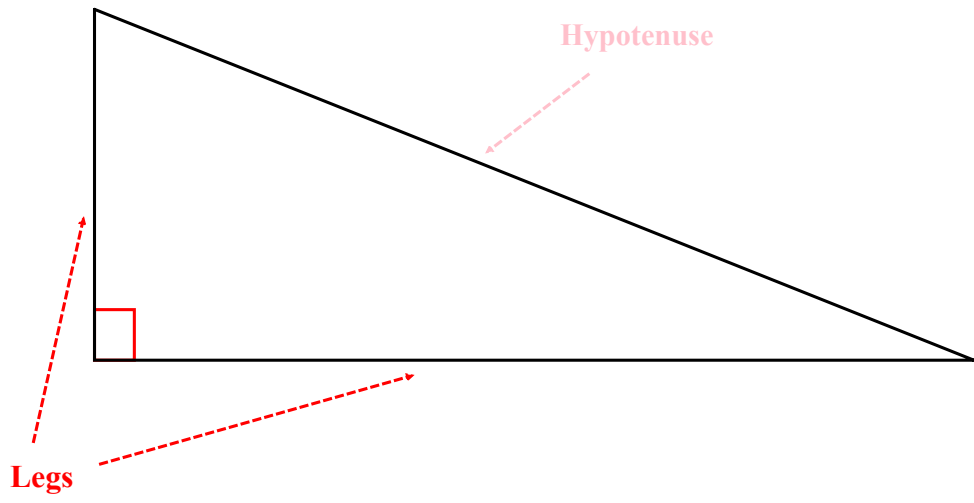
$d = e$
 $3d + 66 = 180$
 $d = 38$
 $e = 38$ $d = e$
 $f = 76$ $e + f + 66 = 180$
 $g = 66$ $f + g + d = 180$
 $h = 104$ $h + 2d = 180$

$k = 76$ suppl \angle 's
 $n = 86$ $d + c + n = 180$
 $p = 38$ $56 + n + p = 180$









Is *SSA* a valid method for proving $\Delta \cong$?

Is *SSA* a valid method for proving $\Delta \cong$?

Nope

Is *SSA* a valid method for proving $\Delta \cong \Delta$?

Nope ... except ...

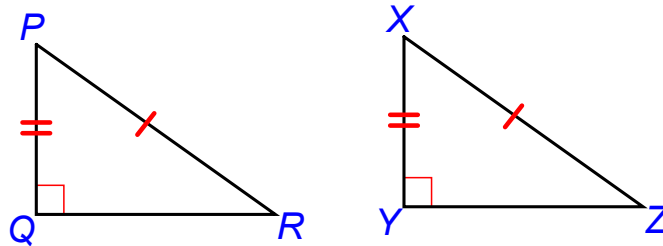
Is *SSA* a valid method for proving $\Delta \cong \Delta$?

Nope ... except ... for one special case ...

Is *SSA* a valid method for proving $\Delta \cong$?

Nope ... except ... for one special case ...

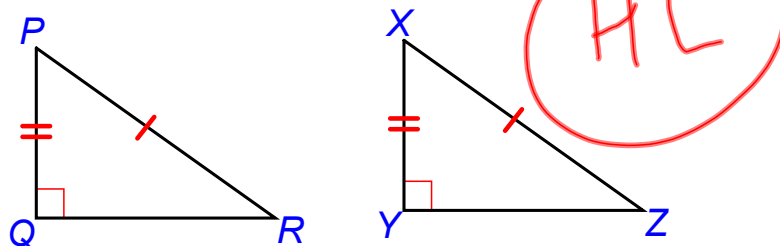
Right triangles ...



Is *SSA* a valid method for proving $\Delta \cong$?

Nope ... except ... for one special case ...

Right triangles ... we call it *Hypotenuse-Leg*

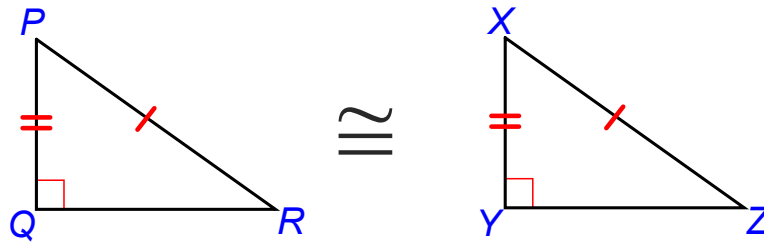


Theorem 4-6: Hypotenuse Leg (HL) Thm

If the hypotenuse & a leg of 1 right Δ are

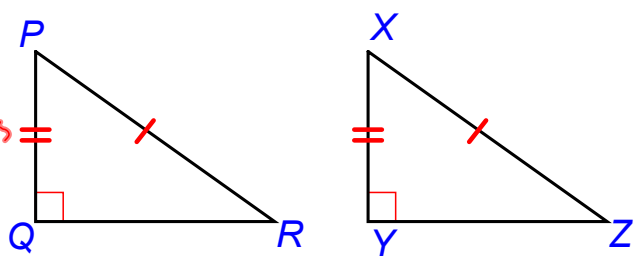
\cong to the hyp. & leg of a 2nd rt Δ

Then the Δ 's are \cong



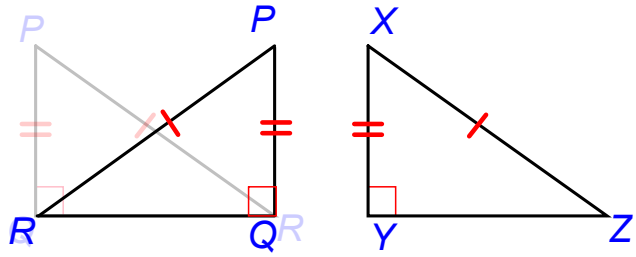
Given $\overline{PR} \cong \overline{XZ}$ Hyp \cong
 $\overline{PQ} \cong \overline{XY}$ 1 pair legs \cong
 $\angle Q$ & $\angle Y$ are rt \angle 's Rt Δ 's

Prove $\Delta PRQ \cong \Delta XZY$



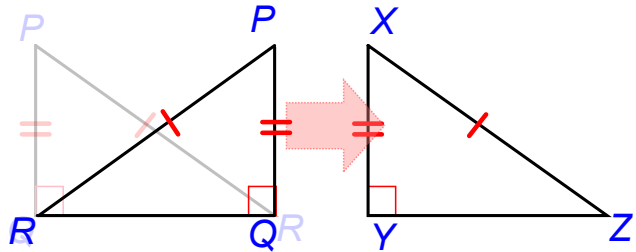
Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$



Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$

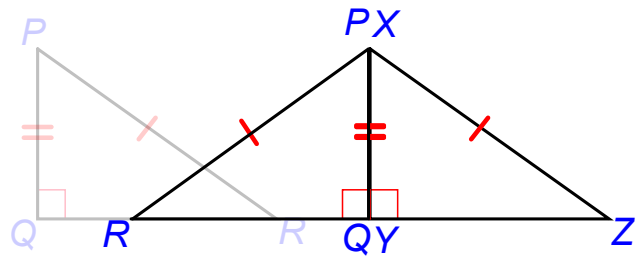


Given $\overline{PR} \cong \overline{XZ}$

$\overline{PQ} \cong \overline{XY}$

$\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$

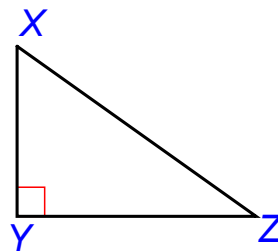
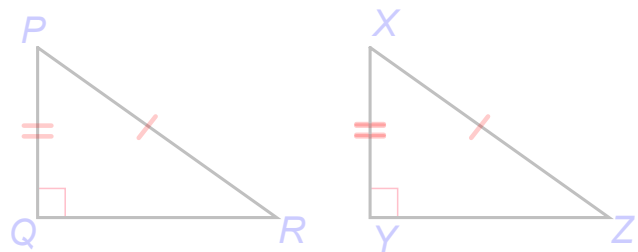


Given $\overline{PR} \cong \overline{XZ}$

$\overline{PQ} \cong \overline{XY}$

$\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$



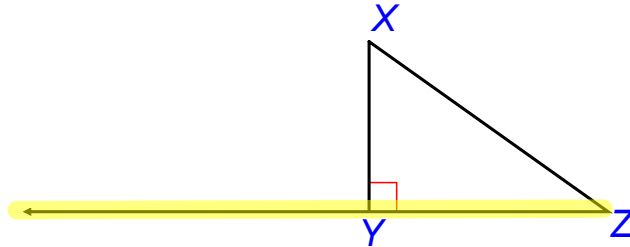
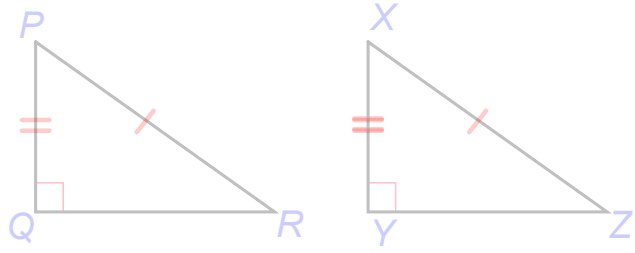
Given $\overline{PR} \cong \overline{XZ}$

$\overline{PQ} \cong \overline{XY}$

$\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$

Construct \overrightarrow{ZY}



Given $\overline{PR} \cong \overline{XZ}$

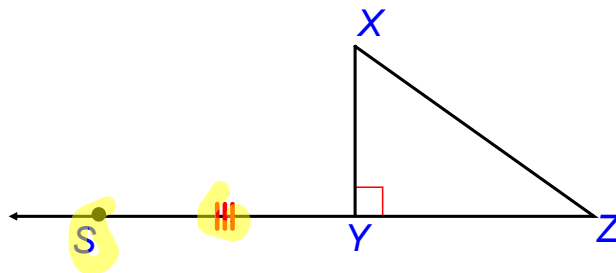
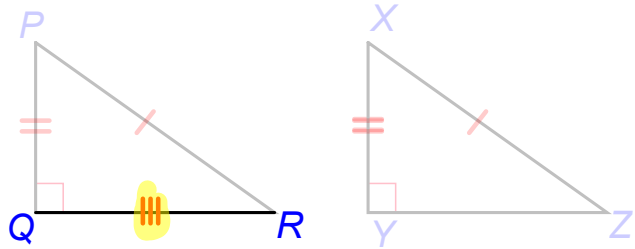
$\overline{PQ} \cong \overline{XY}$

$\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$

Construct \overrightarrow{ZY}

Mark S on \overrightarrow{ZY} so $\overline{YS} \cong \overline{QR}$



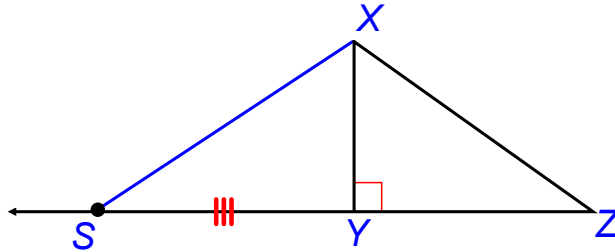
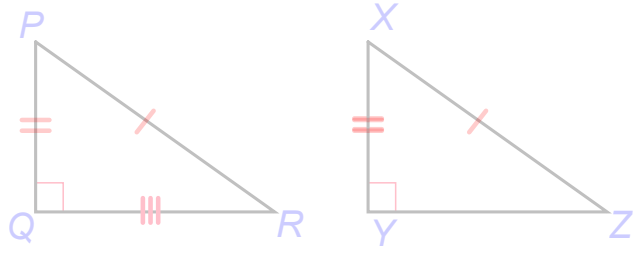
Given $\overline{PR} \cong \overline{XZ}$

$\overline{PQ} \cong \overline{XY}$

$\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$

Construct \overline{ZY}
Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$



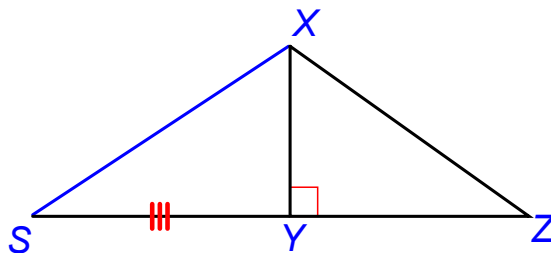
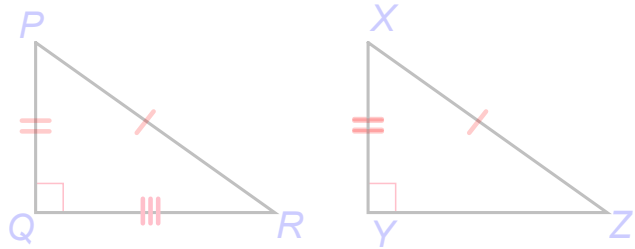
Given $\overline{PR} \cong \overline{XZ}$

$\overline{PQ} \cong \overline{XY}$

$\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$

Construct \overline{ZY}
Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$



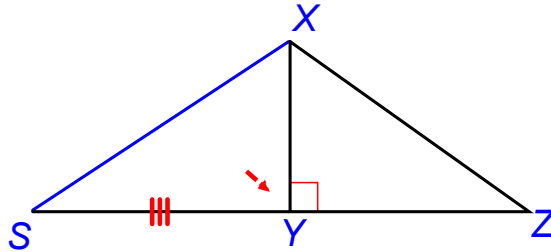
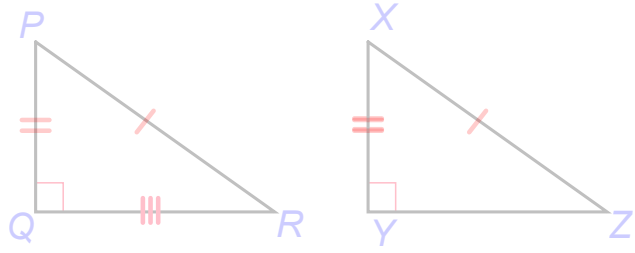
Given $\overline{PR} \cong \overline{XZ}$

$\overline{PQ} \cong \overline{XY}$

$\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$

Construct \overline{ZY}
Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$



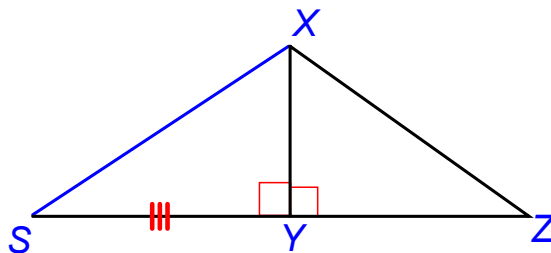
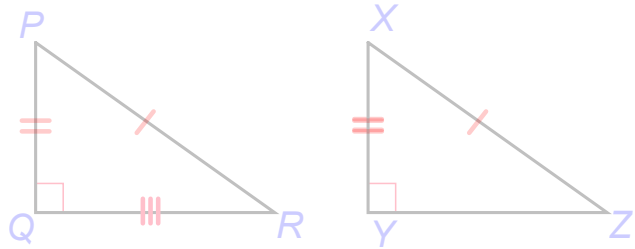
Given $\overline{PR} \cong \overline{XZ}$

$\overline{PQ} \cong \overline{XY}$

$\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$

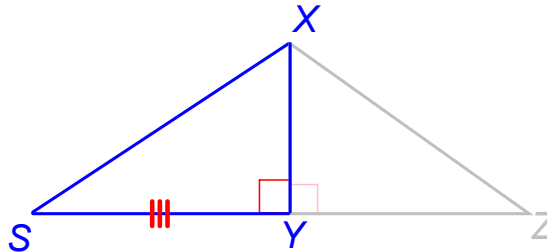
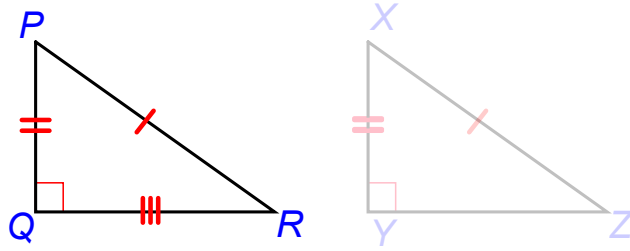
Construct \overline{ZY}
Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$



Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$

Construct \overline{ZY}
 Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$

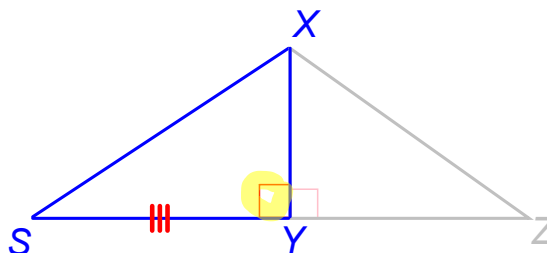
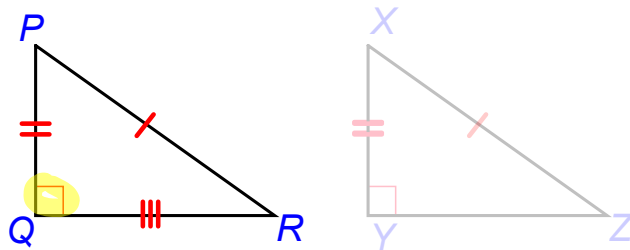


Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$

Construct \overline{ZY}
 Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$

$\angle PQR \cong \angle XYS$ all rt \angle 's \cong

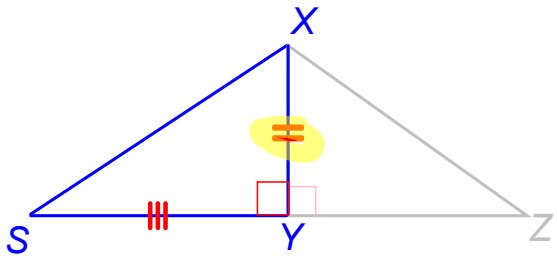
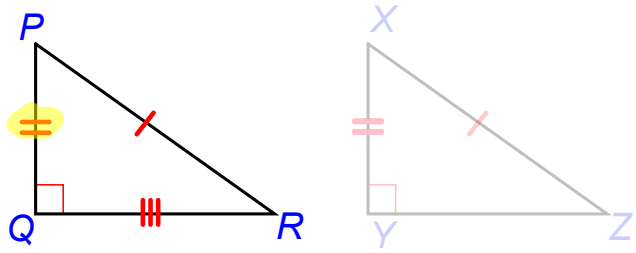


Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$

Construct \overline{ZY}
 Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$

$\angle PQR \cong \angle XYS$ all rt \angle 's \cong
 $\overline{PQ} \cong \overline{XY}$ given

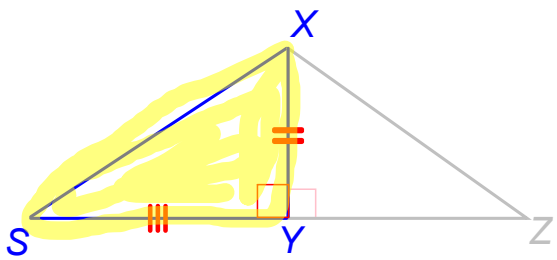
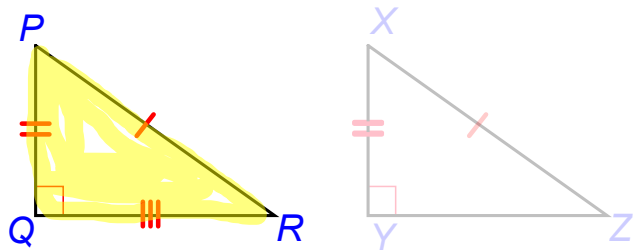


Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$

Construct \overline{ZY}
 Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$

$\angle PQR \cong \angle XYS$ all rt \angle 's \cong
 $\overline{PQ} \cong \overline{XY}$ given
 $\triangle PQR \cong \triangle XYS$ SAS

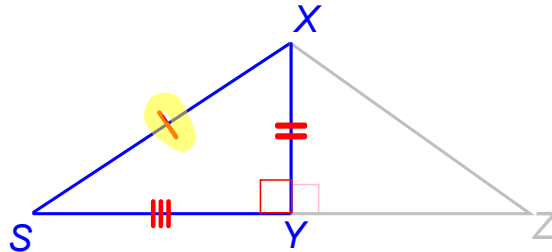
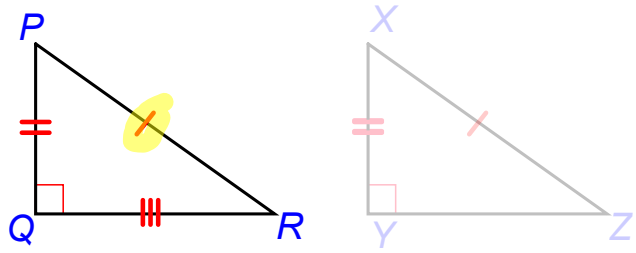


Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\Delta PRQ \cong \Delta XZY$

Construct \overline{ZY}
 Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$

$\angle PQR \cong \angle XYS$ all rt \angle 's \cong
 $\overline{PQ} \cong \overline{XY}$ given
 $\Delta PQR \cong \Delta XYS$ SAS
 $\overline{PR} \cong \overline{XS}$ CPCTC

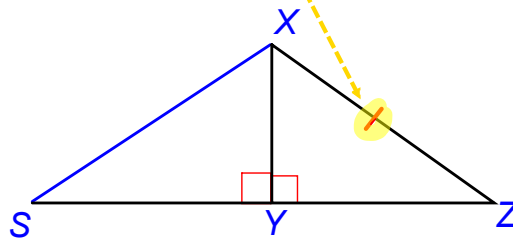
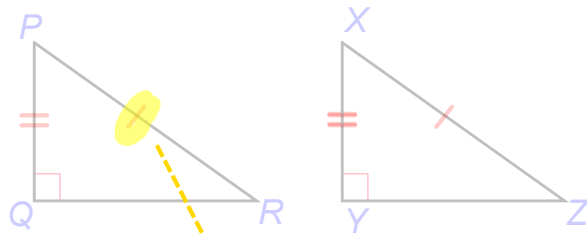


Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\Delta PRQ \cong \Delta XZY$

Construct \overline{ZY}
 Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$

$\angle PQR \cong \angle XYS$ all rt \angle 's \cong
 $\overline{PQ} \cong \overline{XY}$ given
 $\Delta PQR \cong \Delta XYS$ SAS
 $\overline{PR} \cong \overline{XS}$ CPCTC



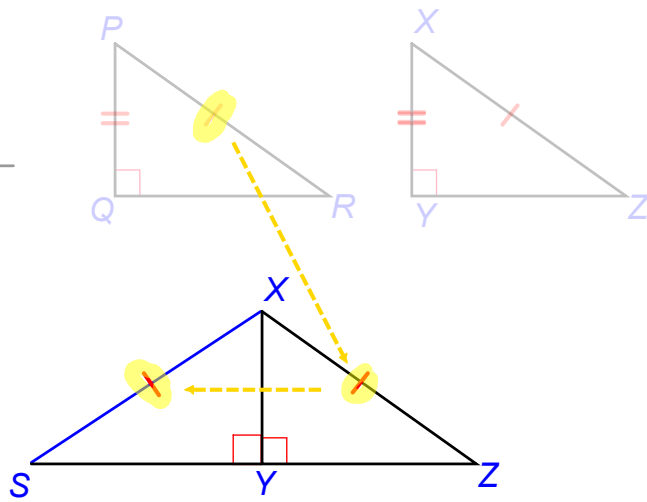
Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$

Construct \overline{ZY}
 Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$

$\angle PQR \cong \angle XYS$ all rt \angle 's \cong
 $\overline{PQ} \cong \overline{XY}$ given
 $\triangle PQR \cong \triangle XYS$ SAS
 $\overline{PR} \cong \overline{XS}$ CPCTC

$\overline{XS} \cong \overline{XZ}$ trans POC



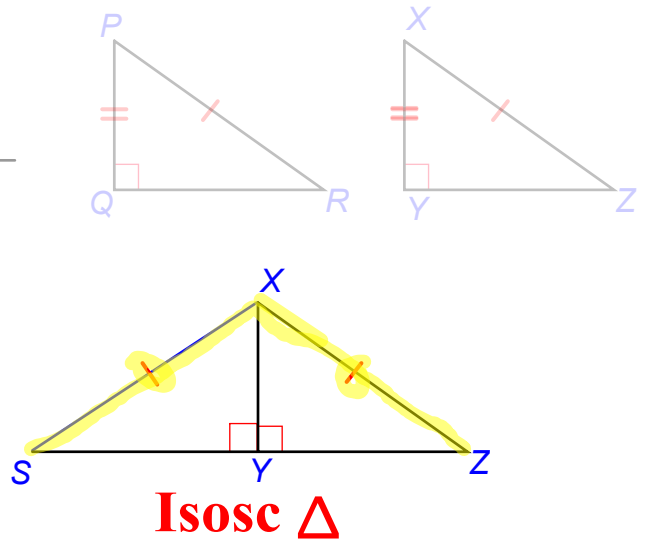
Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$

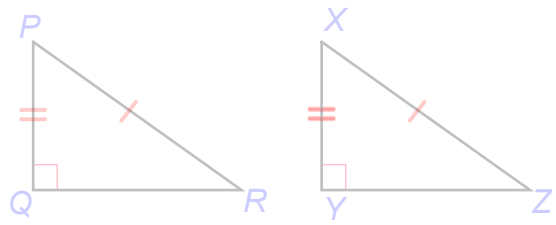
Construct \overline{ZY}
 Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$

$\angle PQR \cong \angle XYS$ all rt \angle 's \cong
 $\overline{PQ} \cong \overline{XY}$ given
 $\triangle PQR \cong \triangle XYS$ SAS
 $\overline{PR} \cong \overline{XS}$ CPCTC

$\overline{XS} \cong \overline{XZ}$ trans POC
 $\triangle SXZ$ is isosceles defn isos \triangle



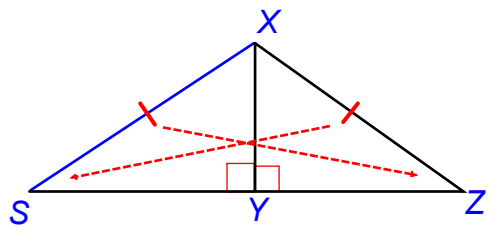
Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's



Prove $\Delta PRQ \cong \Delta XZY$

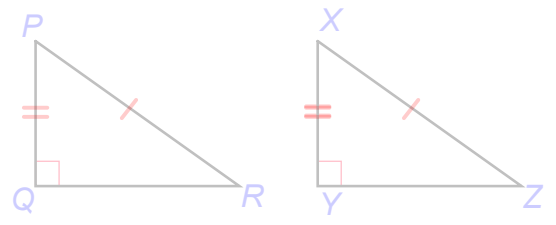
Construct \overline{ZY}
 Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$

$\angle PQR \cong \angle XYS$ all rt \angle 's \cong
 $\overline{PQ} \cong \overline{XY}$ given
 $\Delta PQR \cong \Delta XYS$ SAS
 $\overline{PR} \cong \overline{XS}$ CPCTC



$\overline{XS} \cong \overline{XZ}$ trans POC
 ΔSXZ is isosceles defn isos Δ

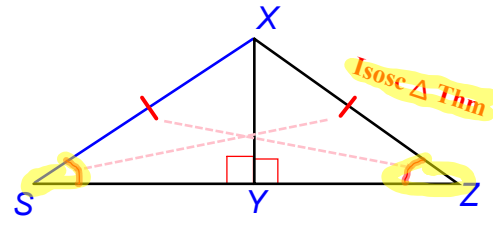
Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's



Prove $\Delta PRQ \cong \Delta XZY$

Construct \overline{ZY}
 Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$

$\angle PQR \cong \angle XYS$ all rt \angle 's \cong
 $\overline{PQ} \cong \overline{XY}$ given
 $\Delta PQR \cong \Delta XYS$ SAS
 $\overline{PR} \cong \overline{XS}$ CPCTC



$\overline{XS} \cong \overline{XZ}$ trans POC
 ΔSXZ is isosceles defn isos Δ
 $\angle S \cong \angle Z$ Isos Δ Thm

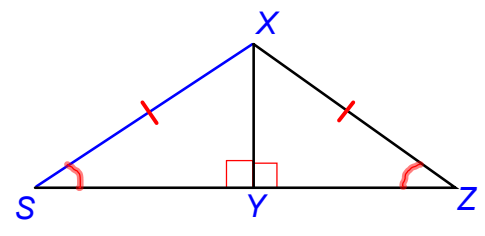
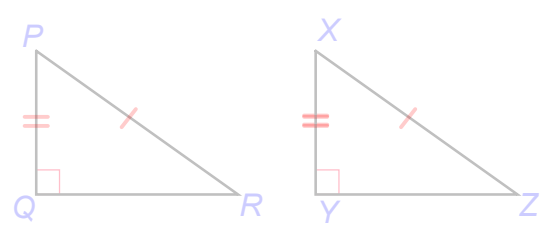
Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\Delta PRQ \cong \Delta XZY$

Construct \overline{ZY}
 Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$

$\angle PQR \cong \angle XYS$ all rt \angle 's \cong
 $\overline{PQ} \cong \overline{XY}$ given
 $\Delta PQR \cong \Delta XYS$ SAS
 $\overline{PR} \cong \overline{XS}$ CPCTC

$\overline{XS} \cong \overline{XZ}$ trans POC
 ΔSXZ is isosceles defn isos Δ
 $\angle S \cong \angle Z$ Isos Δ Thm



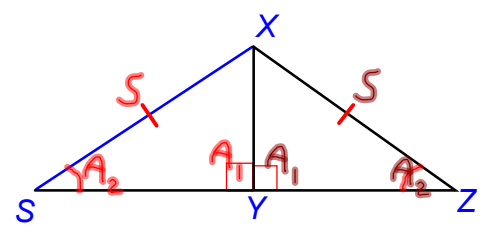
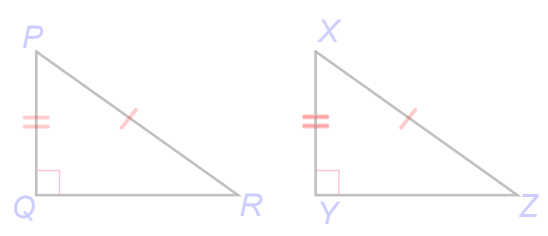
Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\Delta PRQ \cong \Delta XZY$

Construct \overline{ZY}
 Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$

$\angle PQR \cong \angle XYS$ all rt \angle 's \cong
 $\overline{PQ} \cong \overline{XY}$ given
 $\Delta PQR \cong \Delta XYS$ SAS
 $\overline{PR} \cong \overline{XS}$ CPCTC

$\overline{XS} \cong \overline{XZ}$ trans POC
 ΔSXZ is isosceles defn isos Δ
 $\angle S \cong \angle Z$ Isos Δ Thm



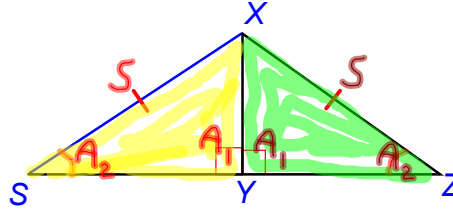
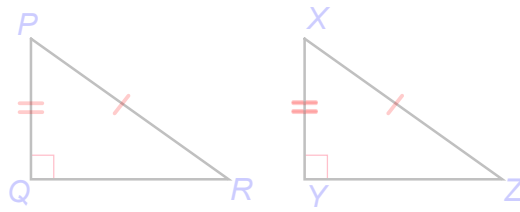
Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$

Construct \overline{ZY}
 Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$

$\angle PQR \cong \angle XYS$ all rt \angle 's \cong
 $\overline{PQ} \cong \overline{XY}$ given
 $\triangle PQR \cong \triangle XYS$ SAS
 $\overline{PR} \cong \overline{XS}$ CPCTC

$\overline{XS} \cong \overline{XZ}$ trans POC
 $\triangle SXZ$ is isosceles defn isos \triangle
 $\angle S \cong \angle Z$ Isos \triangle Thm
 $\triangle XYS \cong \triangle XYZ$ AAS



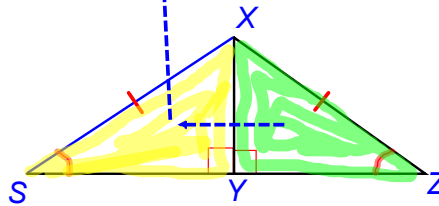
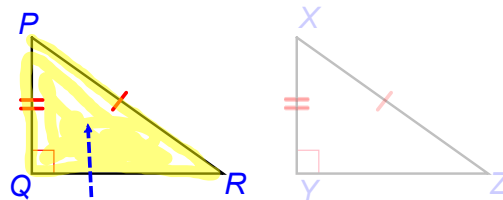
Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's

Prove $\triangle PRQ \cong \triangle XZY$

Construct \overline{ZY}
 Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$

$\angle PQR \cong \angle XYS$ all rt \angle 's \cong
 $\overline{PQ} \cong \overline{XY}$ given
 $\triangle PQR \cong \triangle XYS$ SAS
 $\overline{PR} \cong \overline{XS}$ CPCTC

$\overline{XS} \cong \overline{XZ}$ trans POC
 $\triangle SXZ$ is isosceles defn isos \triangle
 $\angle S \cong \angle Z$ Isos \triangle Thm
 $\triangle XYS \cong \triangle XYZ$ AAS
 $\therefore \triangle PQR \cong \triangle XYZ$ trans POC



Given $\overline{PR} \cong \overline{XZ}$
 $\overline{PQ} \cong \overline{XY}$
 $\angle Q$ & $\angle Y$ are rt \angle 's

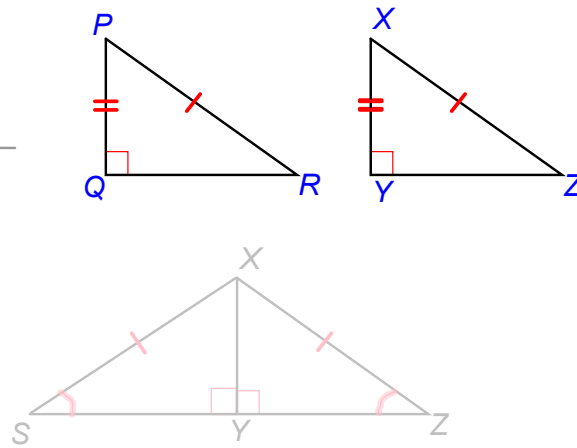
Prove $\triangle PRQ \cong \triangle XZY$

Construct \overline{ZY}
 Mark S on \overline{ZY} so $\overline{YS} \cong \overline{QR}$

$\angle PQR \cong \angle XYS$ all rt \angle 's \cong
 $\overline{PQ} \cong \overline{XY}$ given
 $\triangle PQR \cong \triangle XYS$ SAS
 $\overline{PR} \cong \overline{XS}$ CPCTC

$\overline{XS} \cong \overline{XZ}$ trans POC
 $\triangle SXZ$ is isosceles defn isos \triangle
 $\angle S \cong \angle Z$ Isos \triangle Thm
 $\triangle XYS \cong \triangle XYZ$ AAS
 $\therefore \triangle PQR \cong \triangle XYZ$ trans POC

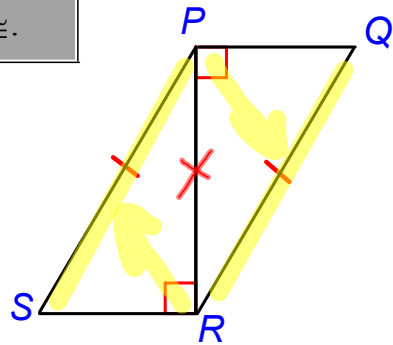
QED



To use the HL Theorem, need to show:

- 1) The 2 \triangle 's are rt \triangle 's
- 2) Hyp \cong
- 3) 1 pair legs \cong

Example - Pg 219 #2: Explain why the 2 Δ 's are \cong .

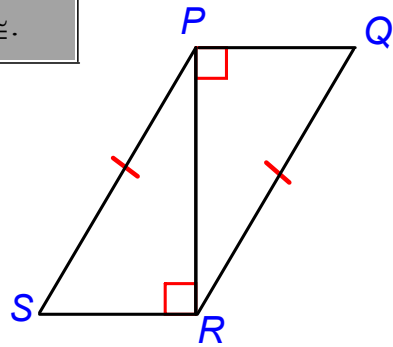


\cong by HL

$\overline{PR} \cong \overline{PR}$ \leftarrow \cong Legs
 $\overline{SP} \cong \overline{PQ}$ \leftarrow \cong Hyp
 $\angle SRP, \angle PQR$ rt \angle 's \leftarrow RT Δ 's

Example - Pg 219 #2: Explain why the 2 Δ 's are \cong .

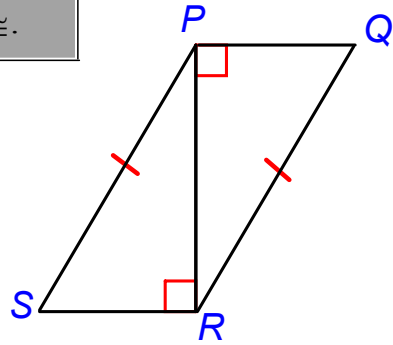
$\Delta SRP \cong \Delta QPR$ by HL Thm



Example - Pg 219 #2: Explain why the 2 Δ 's are \cong .

$\Delta SRP \cong \Delta QPR$ by HL Thm

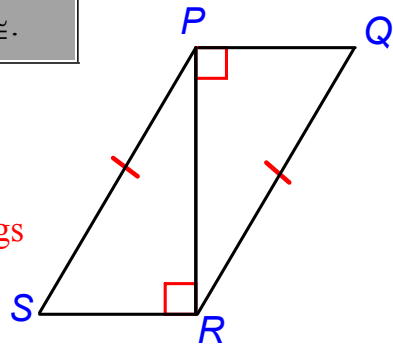
- 1) Show rt Δ 's:
- 2) Show hyp \cong :
- 3) Show legs \cong :



Example - Pg 219 #2: Explain why the 2 Δ 's are \cong .

$\Delta SRP \cong \Delta QPR$ by HL Thm

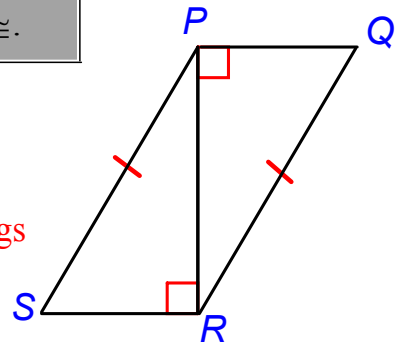
- 1) Show rt Δ 's: $\sphericalangle SRP, \sphericalangle QPR$ rt \sphericalangle 's markings
- 2) Show hyp \cong :
- 3) Show legs \cong :



Example - Pg 219 #2: Explain why the 2 Δ 's are \cong .

$\Delta SRP \cong \Delta QPR$ by HL Thm

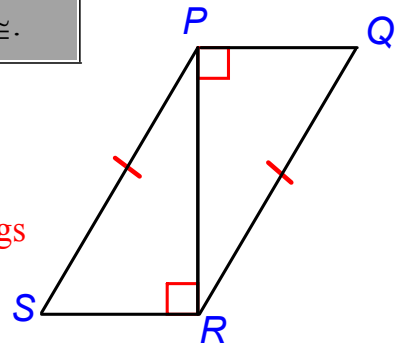
- 1) Show rt Δ 's: $\sphericalangle SRP, \sphericalangle QPR$ rt \sphericalangle 's markings
- 2) Show hyp \cong : $SP \cong RQ$ given
- 3) Show legs \cong :



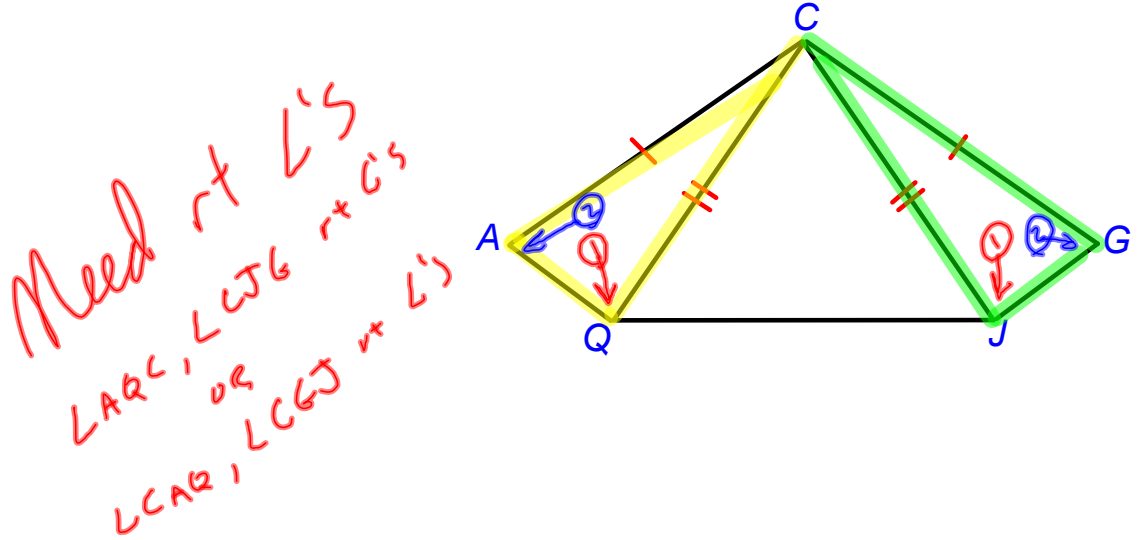
Example - Pg 219 #2: Explain why the 2 Δ 's are \cong .

$\Delta SRP \cong \Delta QPR$ by HL Thm

- 1) Show rt Δ 's: $\sphericalangle SRP, \sphericalangle QPR$ rt \sphericalangle 's markings
- 2) Show hyp \cong : $SP \cong RQ$ given
- 3) Show legs \cong : $PR \cong PR$ refl POC

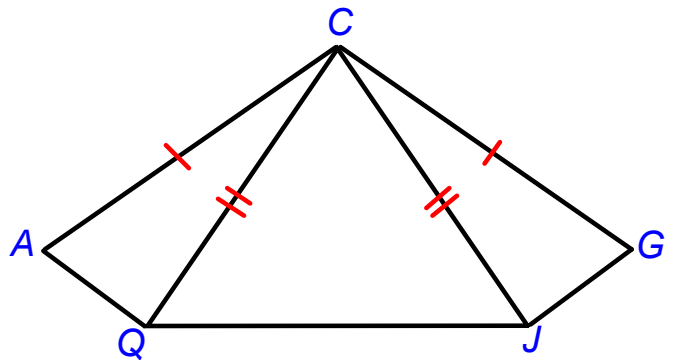


Example - Pg 219 #8: What additional info need to prove $\triangle ACQ \cong \triangle GCJ$ by HL?



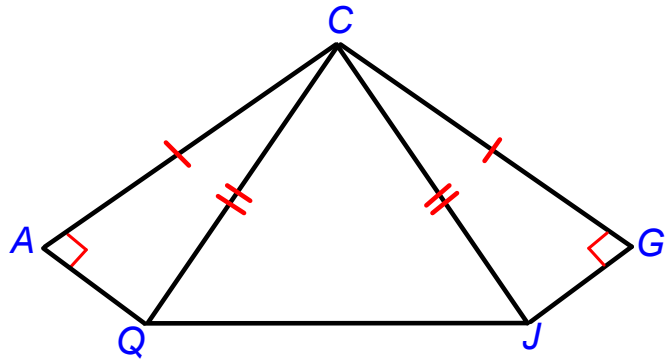
Example - Pg 219 #8: What additional info need to prove $\triangle ACQ \cong \triangle GCJ$ by HL?

Need rt \triangle 's



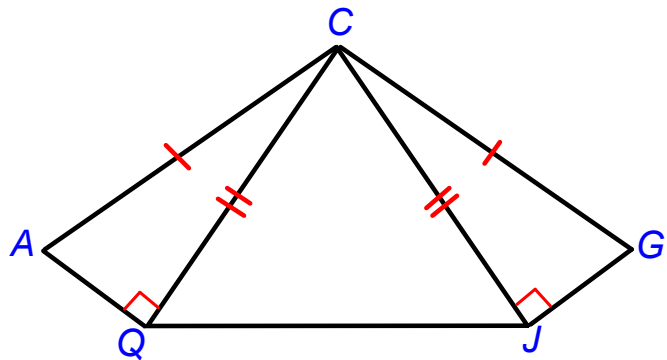
Example - Pg 219 #8: What additional info need to prove $\triangle ACQ \cong \triangle GCJ$ by HL?

Need rt \triangle 's
↓
 $\angle A$ & $\angle G$

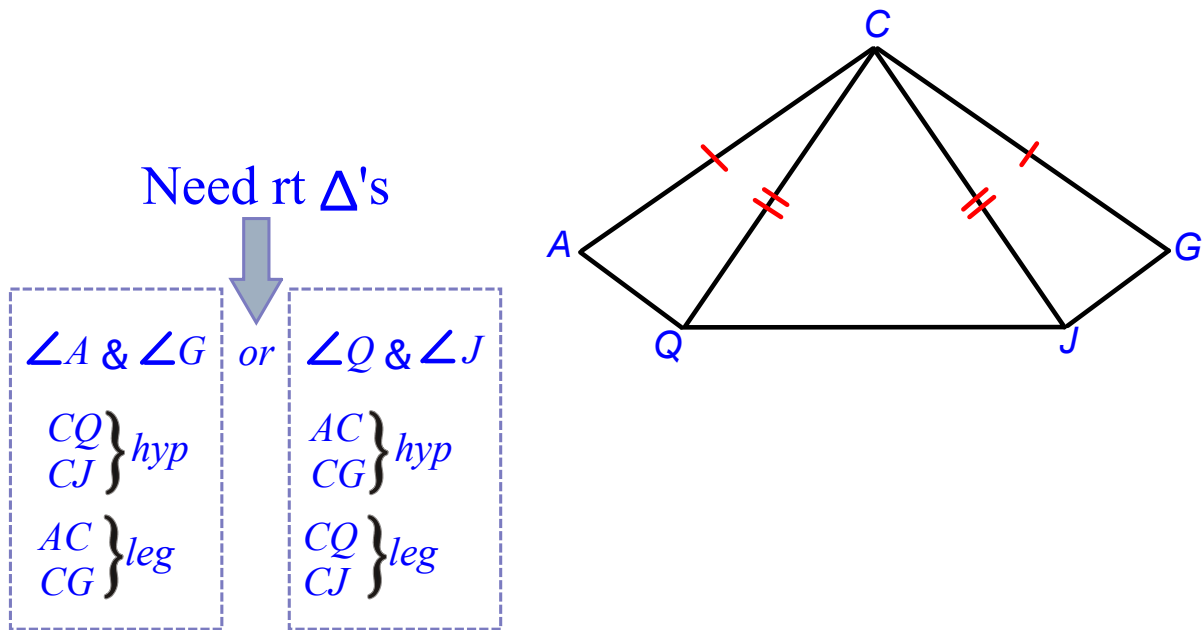


Example - Pg 219 #8: What additional info need to prove $\triangle ACQ \cong \triangle GCJ$ by HL?

Need rt \triangle 's
↓
 $\angle A$ & $\angle G$ or $\angle Q$ & $\angle J$



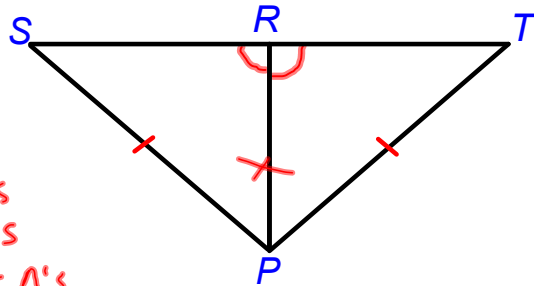
Example - Pg 219 #8: What additional info need to prove $\triangle ACQ \cong \triangle GCJ$ by HL?



Example - Pg 219 #12: Complete the proof

Given $PS \cong PT$ and $\angle PRS \cong \angle PRT$

Prove $\triangle PRS \cong \triangle PRT$



① RT \triangle 's : $\angle SRP, \angle TRP$ are RT \angle 's
 $\rightarrow \cong$ supplements
 $\therefore \triangle SRP, \triangle TRP$ RT \triangle 's

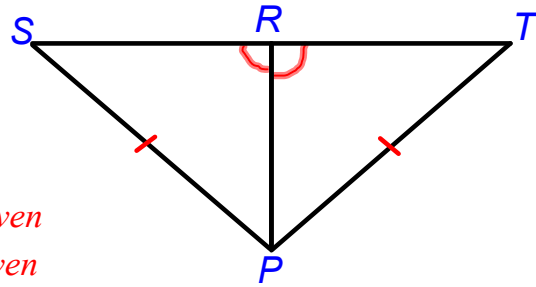
② \cong Hyp: $\overline{SP}, \overline{PT}$ are hyp (opp RT \angle 's)
 $\overline{SP} \cong \overline{PT}$ given (markings)

③ \cong Legs: $\overline{PR} \cong \overline{PR}$ Refl POC

Example - Pg 219 #12: Complete the proof

Given $PS \cong PT$ and $\angle PRS \cong \angle PRT$

Prove $\triangle PRS \cong \triangle PRT$



$\angle PRS \cong \angle PRT$	<i>given</i>
$\angle PRS, \angle PRT$ are supplemental	<i>given</i>
$\angle PRS, \angle PRT$ are rt \angle 's	<i>Thm 2-5</i>
$\triangle PRS$ & $\triangle PRT$ are rt \triangle 's	<i>defn rt \triangle</i>
$\overline{SP} \cong \overline{PT}$ (hypotenuses)	<i>given</i>
$\overline{PR} \cong \overline{PR}$ (legs)	<i>refl POC</i>
$\therefore \triangle PRS \cong \triangle PRT$	<i>HL</i>

QED

Again - to use the HL Theorem, show

- 1) The 2 \triangle 's are rt \triangle 's
- 2) Hyp \cong
- 3) 1 pair legs \cong

L4-6 HW Problems

Pg 219 #1-11 odd,
14-17,
19, 20, 28, 31,
35-46